

## Determination of undrained shear strength and constrained modulus from DMT for stiff overconsolidated clays

ZBIGNIEW LECHOWICZ<sup>1</sup>, SIMON RABARIJOELY<sup>1</sup>, TETIANA KUTIA<sup>2</sup>

<sup>1</sup>Faculty of Civil and Environmental Engineering, Warsaw University of Life Sciences – SGGW

<sup>2</sup>Department of Applied Mathematics, National University of Water and Environmental Engineering, Ukraine

**Abstract:** *Determination of undrained shear strength and constrained modulus from DMT for stiff overconsolidated clays.* The paper presents the results of dilatometer and laboratory tests performed on heavily preconsolidated boulder clays and Pliocene clays prevailing in the Warsaw region. Several different correlations available for evaluating undrained shear strength and constrained modulus from dilatometer tests are discussed. Empirical coefficients for multi-factor correlation to obtain undrained shear strength from dilatometer tests for boulder clays and Pliocene clays were determined. The relationship between factor  $R_M$  and horizontal stress index ( $K_D$ ) for boulder clays was proposed for the evaluation of constrained modulus from dilatometer tests.

*Key words:* cohesive soils, undrained shear strength, constrained modulus, dilatometer test

### INTRODUCTION

The Flat Dilatometer (DMT) was developed in Italy by Silvano Marchetti in 1980 for establishing test methods and original correlations for the evaluation of selected geotechnical parameters. As a load-displacement test, DMT provides very good information on stress history, stiffness and shear strength of soils. It is standardized in Eurocode 7 (1997, 2007) and ASTM (D6635-01 2001, 2007). Detailed information on the DMT equipment, the test procedure and the applied

interpretation formulae are to be found in the DMT 2001 Report by ISSMGE TC16 (2001). A comprehensive update of the above DMT Report, including information on its development in the last 15 years, has recently been published by Marchetti (2015a, b). References concerning DMT can be downloaded from [www.marchetti-dmt.it](http://www.marchetti-dmt.it).

Original correlations for determining geotechnical parameters developed by Marchetti (1980) are in part site-specific and of local character. In original correlations, constrained modulus ( $M$ ) depends on the dilatometer modulus ( $E_D$ ) with a variable coefficient ( $R_M$ ) depending on material index ( $I_D$ ) and horizontal stress index ( $K_D$ ). For the evaluation of undrained shear strength from DMT, Marchetti (1980) developed a correlation based on the relationship between normalized undrained shear strength ( $\tau_{fi}$ ) and overconsolidation ratio ( $OCR$ ) proposed by Ladd et al. (1977), and correlation of  $OCR$  and  $K_D$ .

Comprehensive investigations were made to assess and enlarge the application of DMT in geotechnical engineering (Lutenegger 1988, Powell and Uglow 1988, Lunne et al. 1989, 2006, Monaco and Marchetti 2004, Schnaid 2009, Cao et al. 2015, Robertson 2015, Silvestri

and Tabib 2015, Młynarek et al. 2016). However, in most relationships used to evaluate constrained modulus (Briaud and Miran 1991) and undrained shear strength, intermediate parameters  $I_D$ ,  $K_D$  and  $E_D$  obtained from the DMT readings were commonly used. Roque et al. (1988) proposed an alternative approach for estimating undrained shear strength based on the correlation using  $p_1$  readings and bearing capacity factor ( $N_c$ ). Different approaches were proposed by Yu et al. (1993) and Smith and Houlsby (1995), in which undrained shear strength was a function of the  $p_o$  reading and the bearing capacity factor ( $N_D$ ). Multi-factor correlations were proposed by Rabarijoely (2000) to evaluate undrained shear strength ( $\tau_{fu}$ ), and by Ozer et al. (2006) to evaluate constrained modulus ( $M$ ).

This paper presents the results of dilatometer tests and laboratory tests of heavily overconsolidated boulder clays and Pliocene clays prevailing in the War-

saw region. The problem of evaluating undrained shear strength and constrained modulus from dilatometer tests for heavily overconsolidated clays is discussed. Empirical coefficients for multi-factor correlations to obtain undrained shear strength for boulder clays as well as Pliocene clays are determined. The relationship between  $R_M$  factor and horizontal stress index for boulder clays is proposed for the evaluation of constrained modulus from dilatometer tests.

### DESCRIPTION OF THE TEST SITE

The test site was the II subway line in Warsaw, for which hydrogeological and geotechnical documentation was elaborated by the “Geoteko–WULS–Geoprojekt” Consortium. In 2003–2004, site investigation was carried out for the II subway line comprising 24 stations, 2 standstill stations and 24 tunnels, and in 2009 for

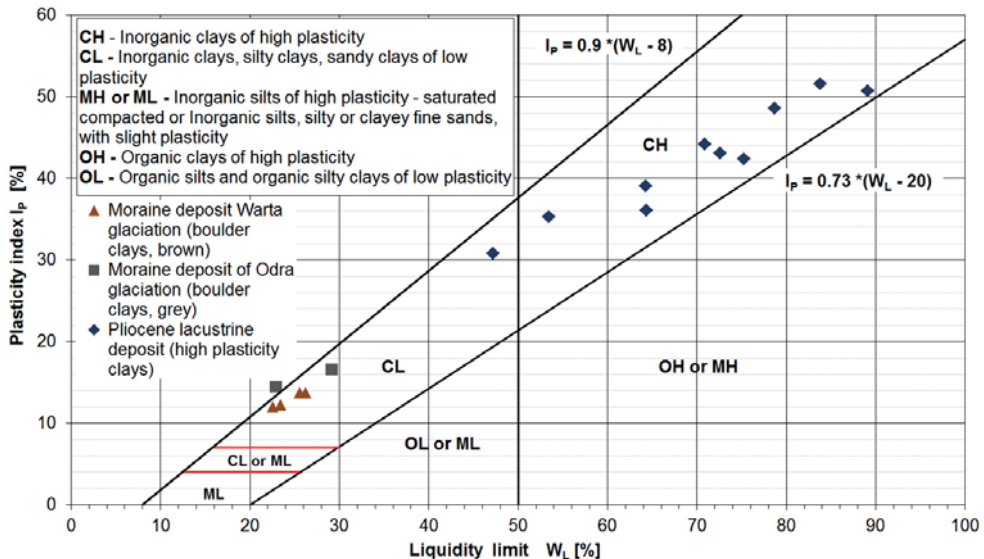


FIGURE 1. Tested soils from the II subway line in Warsaw on Casagrande’s plasticity chart

the II subway line following changes of the planned route, and comprising 20 stations, 2 standstill stations and 20 tunnels. Most of the results of field and laboratory tests shown in this paper are related to the subway stations located in the central part of the II subway line.

In general, the tested subsoil with the exception of surface anthropogenic fill consists of moraine deposits underlain by preglacial deposits or Pliocene clays. Analysis of field and laboratory test results has indicated that the tested soils can be classified as stiff brown boulder clays

of the Warta Glaciation and grey boulder clays of the Odra Glaciation in the upper Quaternary layers, and stiff Pliocene clays in the lower Tertiary layer. Glacial moraine deposits of the Warta and Odra glaciations can be classified as low plasticity clays, and the Pliocene clays as high plasticity clays (Fig. 1). Grain-size distribution of the tested soils is shown in Figure 2. According to Standard EN ISO 14688-1:2002, the boulder clays can be classified as sandy clays (saCL), silty sandy clays (sasiCL) and clayey sands (clSa). Pliocene clays can be classified

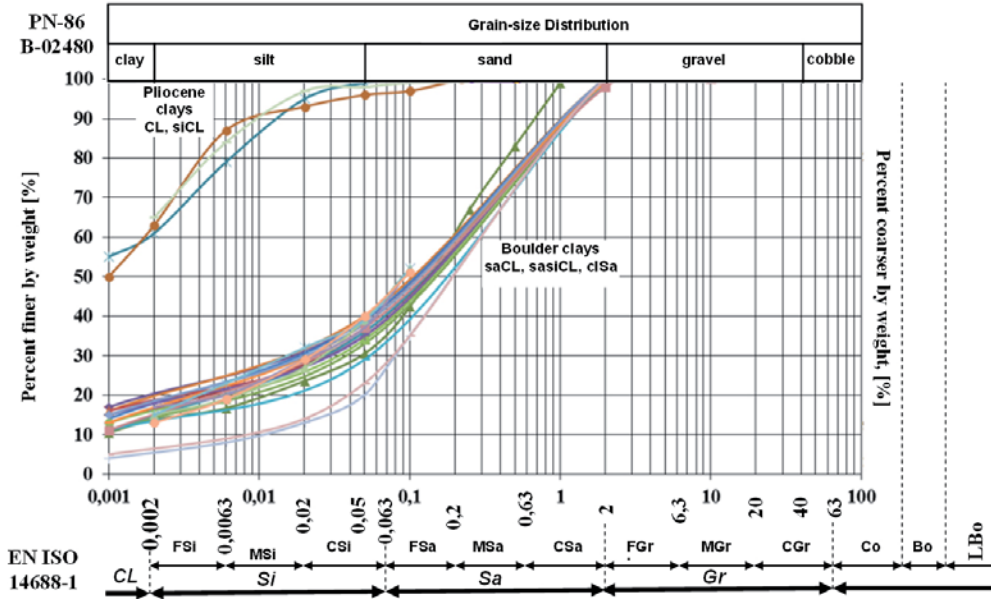


FIGURE 2. Typical grain-size distribution of the tested soils

TABLE. Index properties of the tested soils from the II subway line in Warsaw

Properties	Boulder clay (brown)	Boulder clay (grey)	Pliocene clay	Pliocene silty clay
Water content, $w_n$ (%)	10–14	10–14	18–25	14–20
Unit density, $\rho$ ( $t \cdot m^{-3}$ )	2.1–2.2	2.1–2.2	1.9–2.0	2.0–2.10
Plasticity index, $I_P$ (%)	10–18	10–18	19–64	23–48
Liquidity index, $I_L$ (-)	0.0–0.20	0.0–0.20	-0.10–0.15	-0.10–0.10

as clays (CL) and silty clays (siCL). The index properties of the tested soils are shown in the Table.

### RESULTS OF DMT

Profiles of  $p_o$  and  $p_1$  pressures and index parameters  $I_D$ ,  $K_D$  and  $E_D$  from DMT carried out at the C11 Świętokrzyska station for brown and grey sandy clays, and for Pliocene clay are shown in Figure 3. In the case of the index parameters  $I_D$ ,  $K_D$  and  $E_D$ , the measured values with the average values and  $\pm$  one standard deviation are shown in Figure 3. Results of DMT shown in Figure 4 on Marchetti and Crapps chart (1981)

### EVALUATION OF UNDRAINED SHEAR STRENGTH

Many studies have been performed to evaluate and improve some of the original correlations proposed by Marchetti (1980), however, new correlations are likewise mostly limited to mineral soils (Briaud and Mirian 1991).

The following correlation between normalized undrained shear strength and lateral stress index was proposed by Marchetti (1980) for cohesive soils ( $I_D < 1.2$ ):

$$\frac{\tau_{fu}}{\sigma'_{vo}} = 0,22 (0,5 \cdot K_D)^{1,25} \quad (1)$$

where:

$\sigma'_{vo}$  – *in situ* effective vertical stress.

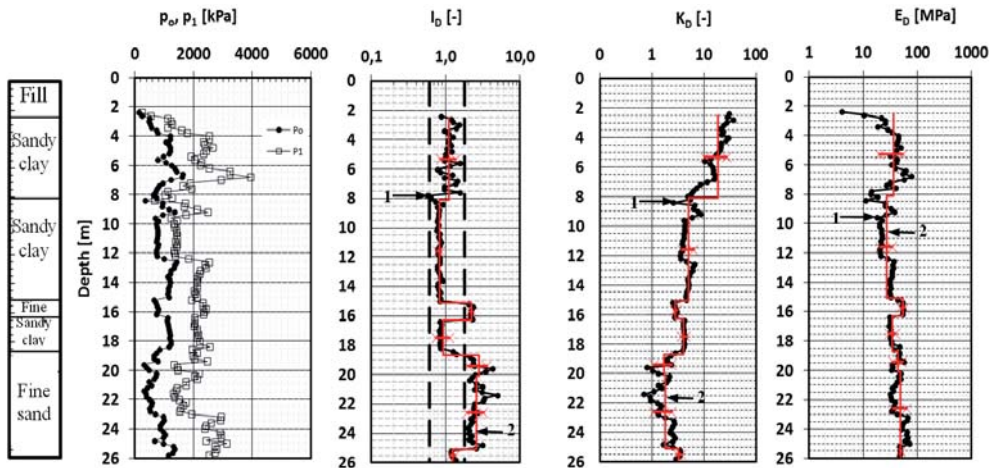


FIGURE 3. Profiles of  $p_o$  and  $p_1$  pressures and index parameters  $I_D$ ,  $K_D$  and  $E_D$  from DMT: 1 – measured values, 2 – average values  $\pm$  one standard deviation

indicate that the tested soils are highly overconsolidated clays.

The analysis carried out by Smith and Housby (1995) indicates that undrained

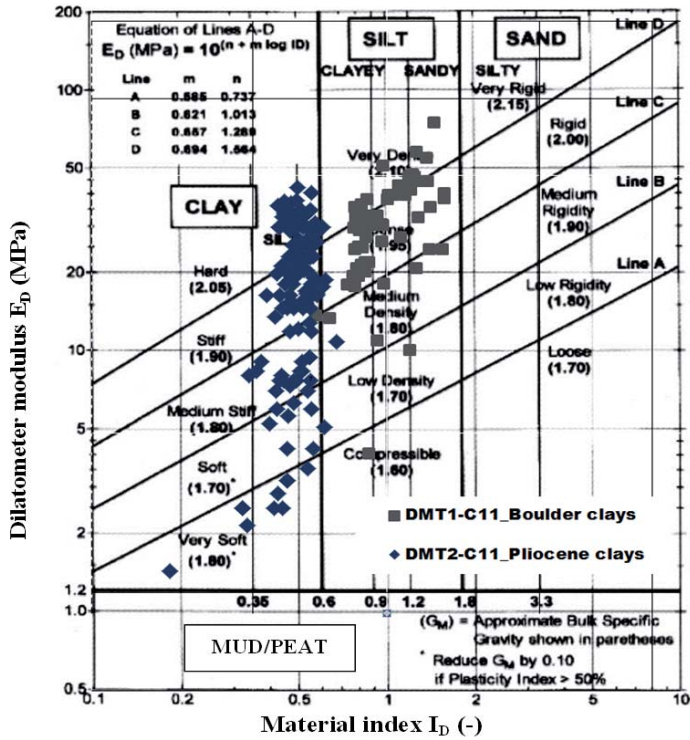


FIGURE 4. Tested soils shown on Marchetti and Crapps chart

shear strength can be estimated from the following formula:

$$\tau_{fu} = \frac{p_o - \sigma_{ho}}{N_D} \quad (2)$$

where:

$p_o$  – corrected first pressure reading;  
 $N_D$  – dilatometer factor for clays, varying from about 4 to 7.

In order to evaluate undrained shear strength in cohesive soils and its variability with depth, comprehensive investigations were undertaken by the Department of Geotechnical Engineering of the Warsaw University of Life Sciences – SGGW (WULS-SGGW). Undrained shear strength was determined in the laboratory in triaxial tests on undisturbed

samples. In laboratory tests for samples taken from the tested area, a criterion for acceptable volumetric strain for the reconsolidation to *in situ* effective stress was used to determine the quality of the tested soil specimens.

Analysis of DMT results indicates that, particularly for boulder clays, the relationship between normalized undrained shear strength and horizontal stress index ( $K_D$ ) differs from that proposed by Marchetti in 1980 (Fig. 5).

The following modified correlation between normalised undrained shear strength and horizontal stress index for boulder clay is proposed (Fig. 5):

$$\frac{\tau_{fu}}{\sigma'_{vo}} = 0.22 \cdot (0.5 \cdot K_D)^{1.12} \quad (3)$$

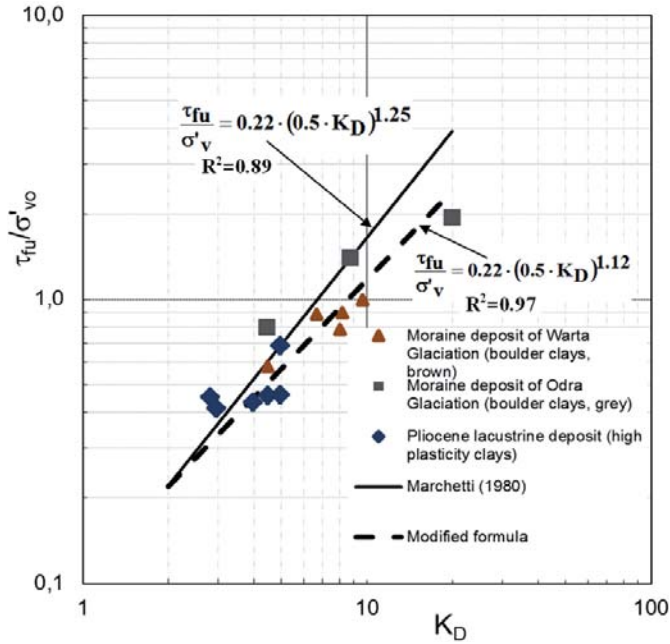


FIGURE 5. Relationship between normalized undrained shear strength ( $\tau_{fu}$ ) and horizontal stress index ( $K_D$ )

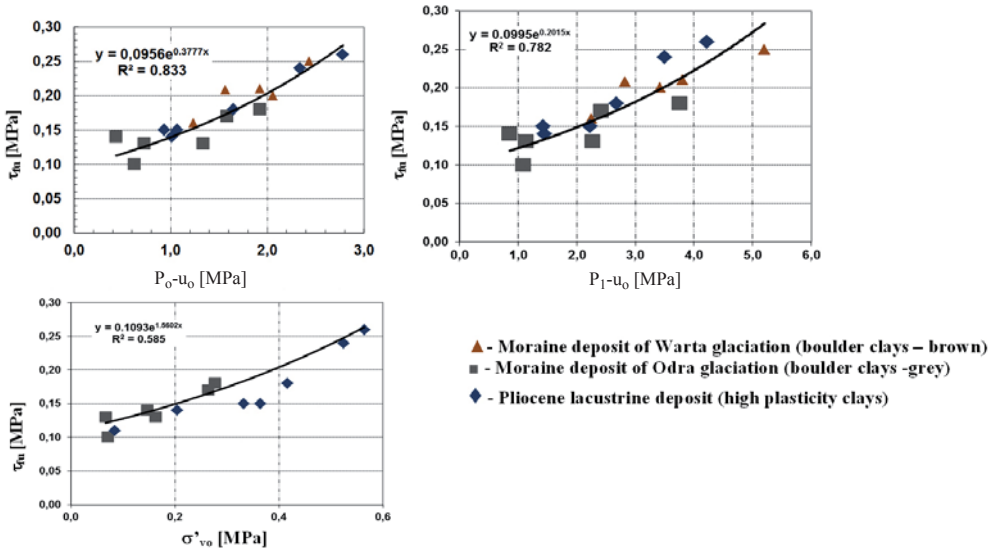


FIGURE 6. Undrained shear strength ( $\tau_{fu}$ ) versus  $p_1 - u_0$ ,  $p_0 - u_0$  and  $\sigma'_{v0}$

In Figure 6, undrained shear strength is correlated with different factors (difference between  $p_o$  and  $u_o$ ; difference between  $p_1$  and  $u_o$ ; effective vertical stress) similarly as in Rabarijoely (2000) and Ozer et al. (2006). Multiple regression analysis indicates quite good correlation, however a considerably lower  $R^2$  value was obtained for the relationship between undrained shear strength and effective vertical stress.

Experience from organic soils indicates that for the evaluation of undrained shear strength from dilatometer tests, the following formula proposed by Rabarijoely (2000) can be used:

$$\tau_{fu} = \alpha_0 \sigma'_v \alpha_1 \cdot (p_o - u_o)^{\alpha_2} \cdot (p_1 - u_o)^{\alpha_3} \quad (4)$$

where:

- $\sigma'_v$  – effective vertical stress;
- $u_o$  – *in situ* pore water pressure;
- $\alpha_0, \alpha_1, \alpha_2, \alpha_3$  – empirical coefficients.

Analysis of test results indicates that the obtained values of empirical coefficients for formula (4) for boulder clays and Pliocene clays from the Warsaw region are  $\alpha_0 = 0.18$ ,  $\alpha_1 = 0.14$ ,  $\alpha_2 = 0.20$ , and  $\alpha_3 = 0.15$ .

In order to evaluate undrained shear strength from dilatometer tests, formula (4) with obtained values of empirical coefficients was used. A comparison between undrained shear strength obtained from triaxial tests and dilatometer tests for boulder clays and Pliocene clays from the Warsaw region is shown in Figure 7. In general, there is a good agreement between the evaluated undrained shear strength based on the multifactor relation and values obtained from triaxial tests.

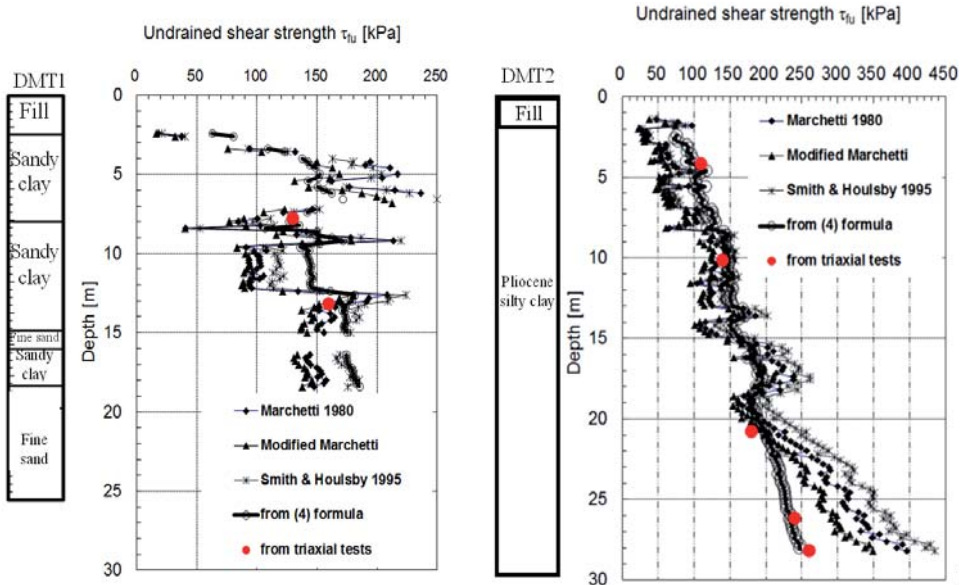


FIGURE 7. Profiles of undrained shear strength ( $\tau_{fu}$ )

### EVALUATION OF CONSTRAINED MODULUS

In order to evaluate constrained modulus from dilatometer tests, the empirical correlations proposed by Marchetti (1980) are as follows:

$$M = R_M \cdot E_D \tag{5}$$

$$I_D \leq 0.6$$

$$R_M = 0.14 + 2.36 \cdot \log K_D \tag{6}$$

$$0.6 < I_D < 3.0$$

$$R_M = 0.14 + 0.36 \cdot \left( \frac{I_D - 0.6}{2.4} \right) + \left[ 2.5 - \left( 0.14 + 0.36 \cdot \frac{I_D - 0.6}{2.4} \right) \right] \cdot \log K_D \tag{7}$$

where:

$R_M$  – factor related to horizontal stress index –  $K_D$  (-);

$E_D$  – dilatometer modulus (MPa);

$I_D$  – material index (-).

Analysis of DMT results and oedometer tests shows that for boulder clays the relationship between factor  $R_M$  and index  $K_D$  differs from that proposed by Marchetti in 1980 (Fig. 8). Comparison of the constrained modulus obtained from oedometer tests during reloading indicates that for interpretation of dilatometer tests in boulder clays, the following relation can be used for determination of the factor  $R_M$ :

$$R_M = 0.14 + 1.6 \cdot \log K_D \tag{8}$$

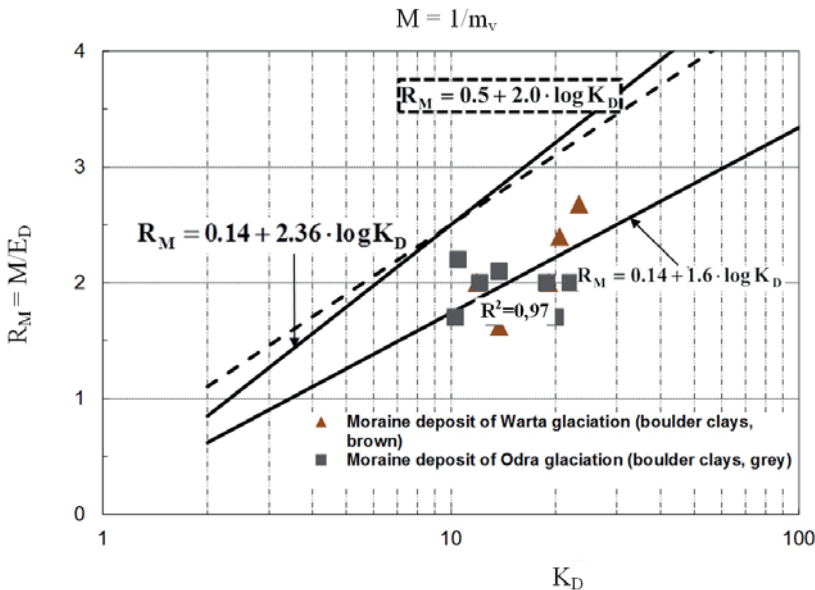


FIGURE 8. Factor  $R_M = M/E_D$  versus  $K_D$



## CONCLUSIONS

The paper presents the problem of accuracy in evaluating undrained shear strength and constrained modulus of heavily overconsolidated cohesive soils from dilatometer tests. A comparison between undrained shear strength from dilatometer tests evaluated from formulae presented in literature and undrained shear strength obtained from triaxial tests indicates significant differences. Empirical coefficients for boulder clays and Pliocene clays were determined for multi-factor correlation proposed by Rabarijoely (2000) used to obtain undrained shear strength from dilatometer tests. Analysis of DMT results and oedometer tests shows that for boulder clays the relationship between factor  $R_M$  and index  $K_D$  differs from that proposed by Marchetti (1980). The relationship between factor  $R_M$  and index  $K_D$  for boulder clays was proposed for evaluation of  $M$  from dilatometer tests.

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**Streszczenie:** Wyznaczenie wytrzymałości na ścinanie bez odpływu i modułu ściśliwości z badań DMT silnie prekonsolidowanych ilów. W artykule przedstawiono wyniki badań dylatometrycznych i badań laboratoryjnych silnie prekonsolidowanych morenowych gruntów spoistych zlodowacenia Warty i Odry oraz ilów plioceńskich występujących na trasie II linii metra w Warszawie. Przedstawiono porównanie wartości wytrzymałości na ścinanie bez odpływu ( $\tau_{fi}$ ) badanych gruntów spoistych uzyskanych z badań dylatometrycznych, wykorzystując prezentowane w literaturze zależności empirycznych z wartościami wyznaczonymi z badań trójosiowych. Analiza wyników badań pozwoliła na określenie wartości współczynników empirycznych do wieloczynnikowej zależności zaproponowanej przez Rabarijoely'ego w 2000 roku, służącej wyznaczeniu wytrzymałości na ścinanie bez odpływu na podstawie badań dylatometrycznych. Porównanie wyników badań dylatometrycznych z wynikami badań edometrycznych wskazuje na istotne różnice między uzyskanymi wynikami a zależnością podaną przez Marchettiego w 1980 roku. Dla morenowych gruntów spoistych zlodowacenia Warty i Odry podano zależność empiryczną między wskaźnikiem  $R_M$  a wskaźnikiem naprężenia bocznego ( $K_D$ ) wykorzystywaną w wyznaczeniu z badań dylatometrycznych modułu ściśliwości ( $M$ ).

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**Authors' addresses:**

Zbigniew Lechowicz, Simon Rabarijoely  
Katedra Geoinżynierii  
Wydział Budownictwa i Inżynierii Środowiska  
SGGW  
ul. Nowoursynowska 159, 02-776 Warszawa  
Poland  
e-mail: zbigniew\_lechowicz@sggw.pl  
simon\_rabarijoely@sggw.pl

Tetiana Kutia  
Department of Applied Mathematics  
National University of Water and Environmental  
Engineering  
11 Soborna Str., 33028 Rivne  
Ukraine  
e-mail: kutetiana@gmail.com